

# Research Article Investigation of plastic hinge length in high-ductility reinforced concrete shear walls

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Abstract: In this study, the plastic hinge lengths of reinforced concrete (R/C) cantilever shear walls were analytically determined considering various design parameters. Nonlinear static (Pushover) analyses were conducted on R/C shear wall models and their nonlinear behavior was examined using ABAOUS software. In the study, 72 shear wall models with different parameters were analyzed under the influence of vertical and horizontal loads. Parameters whose effects on plastic hinge length were investigated height/length ratio (H<sub>w</sub>/L<sub>w</sub>), axial load ratio (N/N<sub>o</sub>), and horizontal web reinforcement ratio  $(\rho_{sh})$ . The load-displacement graphs of the modelled shear walls were obtained. The plastic hinge height of shear walls was determined according to the heights of the deformations in the concrete and longitudinal steel reinforcement in the section when the shear walls lateral load decreased by 15%. The analytical plastic hinge lengths (L<sub>pz</sub>) were determined with respect to the location of the yield occurred at the longitudinal steel reinforcement of the shear wall. The observed plastic hinge lengths (Lp) were determined based on the height of observed the crush as of the foundation top level in the concrete shear wall model. The relationship between the findings of this study and empirical formulas in the literature was determined. It was determined that there is greater closeness between the values obtained from empirical formulas in the literature and the observed plastic hinge length values. It was observed that the plastic hinge length generally increases as the shear span increases. It was observed that the change in  $\rho_{sh}$  was not a very effective parameter in plastic hinge formation. As the N/N<sub>o</sub> decreases, the plastic hinge length values generally increase. The  $L_p/L_{pz}$  ratio varied within the range of 0.15-0.50. In addition to ductility ( $\mu$ ) values were determined by using the displacements determined according to both the crushing occurred in the shear wall concrete and the yield observed in the steel reinforcement. The observed that the ductility value depends more on  $H_{\rm w}/L_{\rm w}$  ratio as  $N/N_{\rm o}$  ratio decreases.

Keywords: Earthquake, failure, plastic hinge, finite elements, shear wall.

### 1. Introduction

Mechanical models that can predict the analytical load-deformation relationship with sufficient accuracy must be used for the evaluation of the behavior of the reinforced concrete structures under earthquake. In order to obtain the more realistic load-displacement relationship of structures, the behavior of non-linear regions must be modeled within the framework of a set of rules. In the computer models of structures, plastic hinge assumptions are made for the regions where plastic deformations are anticipated to occur. In a plastic hinge of reinforced concrete section, the reinforcement in the tension zone must first yield and then the concrete in the compression zone must be crushed with the increasing curvature demand. The region where the plastic hinge forms and the height (length) of the plastic hinge are extremely important to determine the global performance of a structure. Aksoylu et al. (2020) conducted pushover analyses for structures with different story heights and investigated the formation of plastic hinges Eslami & Ronagh (2014), Değer & Başdoğan (2020) stated that the features adopted for the plastic hinge change the load-displacement relationship of a structure. In order to obtain the accurate load-displacement relationship of a building, the hinge-development features of shear walls, columns and beams, which form the load carrying system, are important. Moreover, it is also known that especially shear walls play an important role in the horizontal load bearing capacity and the ductility of a building during earthquake.

Reinforced concrete shear walls are frequently preferred in countries with high seismic activity in order to increase the horizontal stiffness of the structural system and to reduce the displacements taking place during the earthquake and the damages associated with them (Sorosh & Sari (2022)). In order to ensure the performance expected from shear walls during earthquake is achieved, it is extremely important to design the shear walls with adequate reinforcement and place them at appropriate locations within the building. Field observations after earthquakes, such as 06 Şubat 2023 Kahramanmaraş Earthquake Doublets (7.8 M<sub>w</sub> and 7.6 M<sub>w</sub> in Turkey) have documented that malpractice actions in especially improperly selection of shear wall locations, inadequate reinforcement detailing and weak workmanship for concrete triggered to damage (Marius, 2013; İTÜ, 2023; Oztürk et al., 2023). Similarly, Kam et al. (2011) and Ozdemir et al. (2021) point out, especially based on their field observations made after earthquakes, that there were not enough shear walls in the buildings where high damage and destruction occurred. In the Turkish Building Earthquake 2018 (TBEC-2018) and other previous versions, no shear wall area condition is given depending on the building height and ground floor area (except for tunnel formwork buildings). Additionally, there are empirical approaches considering wall density in the literature (Kazaz, 2016; Soydaş, 2009; Alkazan, 2020; Burak & Comlekoglu, 2013) recommendations are given about the amount of shear walls to prevent the collapse of a reinforced concrete building.

There are different studies in the literature on the seismic behavior of shear walls. Gallegos et al. (2023) evaluated the seismic collapse behavior of high-rise RC dual-wall-frame buildings located on moderately stiff soil. Sritharan et al. (2014) investigated the weaknesses and design principles of shear walls in earthquake behavior. Henry (2013), Lu et al. (2017), Encina et al. (2016), Lu et al. (2018) examined the effect of longitudinal reinforcement placement in shear walls on behavior. Dazio et al. (2009) investigated different vertical reinforcement and ductility content in shear wall. Kazaz (2013), Takahashi et al. (2013), Massone & Alfaro (2016), Foroughi & Yüksel (2020) investigated the effects of changing parameters on the nonlinear behavior of shear walls. Cai et al. (2024) investigated the plastic hinge lengths of flanged reinforced concrete walls using the finite element method. They proposed equations for determining the plastic hinge length by taking into account the effects of different parameters. Jun (2014) investigated the damage conditions of the shear wall with the fiber element method. The general purpose of these studies is to determine the parameters that affect the seismic behavior of shear walls. In addition, determination of plastic hinge height has been the main motivation subject.

In order to dissipate energy, the structure needs to undergo plastic deformations during an earthquake. In regions where plastic deformations occur, crushing in concrete deformations in compression zone can be observed from the outside of shear walls, whereas it is not possible to observe starting point of steel longitudinal bars yield deformations. In other words, in the section, the plastification starts from the point where the reinforcement yields and it is impossible to observe this length from the outside. If concrete and reinforcement damage are evaluated separately, plastic hinge height can be considered in two ways as the height at which the concrete is crushed (observed height,  $L_p$ ) and the height at which the reinforcement longitudinal bars start to yield (analytical height,  $L_{pz}$ ). However, the number of studies investigating the relationship between  $L_p$  and  $L_{pz}$  depending on the parameters is very limited.

Observations made in the field after earthquakes and data obtained from experimental studies indicate differences between the plastic hinge length  $L_p$  obtained from external observation and the plastic hinge length  $L_{pz}$  formed starting from the section where longitudinal reinforcement is yielded (Priestley et al. 2007; Bohl and Adebar, 2011). Certainly, it is evident that in experimental studies, deformation measurement can be performed by placing strain gauges on longitudinal reinforcements close to the outermost fiber in the tension zone (Dazio et al., 2009). However, experimental data on this is quite limited. Especially in experiments, the negative effect of strain-guage placement on bond challenges researchers on this issue (Hoffmann, 2012; Clauß et al., 2020). In this respect, by calculating the distance to the foundation of the sections where the reinforcement yielded and the concrete begins to crush, with developed FEM methods, the lengths of both plastic hinges ( $L_p$  and  $L_{pz}$ ) can be calculated without performing experiments.

There are many parameters depending on the properties of the shear wall that affect the difference between  $L_p$  obtained from observed and  $L_{pz}$  obtained analytically. The main purpose of this study is to see the interaction between  $L_p$  and  $L_{pz}$ . In other words, it is very important to calculate the relationship between the plastic hinge height  $L_p$ , formed by crushing the concrete, and the final section height  $L_{pz}$ , where the reinforcement yielded, through a non-linear FEM model developed. In the study, also aimed to compare the relationship between the  $L_p$  and  $L_{pz}$  values obtained from empirical formulas in the literature and the values founded in this study.

For this reason, in the study, it was aimed to analytically (by using FEM) determine the plastic hinge lengths of highductility shear walls. The numerical analysis provides a deeper understanding of the structural behavior and allows collecting data which is difficult to record during the experiments and it is utilized as an alternative to the experimental study by many researchers (Pokhrel and Bandelt (2019), Barbagallo (2022). It is preferred various software to examine building behavior in the literature. Zhao et al. (2011) used the DIANA program to examine the plastic hinges formed in beams in terms of element dimensions, reinforcement ratio and material properties. Zhang et al. (2022) examined the behavior of prestressed concrete composite shear walls according to various parameters with Abaqus software. Mamdouh et al. (2022) used the ANSYS finite element program to examine the behavior of reinforced concrete shear walls with discontinuities. In this present study, numerical analyses were performed using a finite element tool, ABAQUS, to deeply investigate the effects of the parameters on  $L_p$  and  $L_{pz}$  of ductile reinforced concrete shear walls. In this study, concrete and material models were selected by the authors from models previously used in the verification of various experimental studies.  $L_p$  and  $L_{pz}$  interpretations were made based on the damage distribution and deformation profile obtained as a result of the analysis of 72 different shear walls. Moreover the shear walls were modeled by ABAQUS software and the load-displacement graphs of each shear wall were obtained. Despite there are many studies in the literature about shear wall  $L_p$  and  $L_{pz}$  lengths, the associations made based on concrete and reinforcement deformation through the FEM-model used and the commentations made about  $\mu_{\delta}$  have not been discussed in the literature. Therefore, the novel part of the study is to obtain the  $L_p$  and  $L_{pz}$  relationship depending on concrete and reinforcement deformation, and to examine the L<sub>p</sub> and L<sub>pz</sub> relationship according to the changing parameters in this context. From this motivation, first of all based on a shear wall sample tested in the literature, the numerical model verified. After that seventy-two (72) shear walls were designed and modeled according the requirements stipulated in the TBEC-2018 and selected parameters. While determining the parameters whose effects will be examined, the literature was examined. The studies have shown that there are different expressions for the plastic hinge length for each distinct parameter such as wall length (L<sub>w</sub>), wall height (H<sub>w</sub>), axial load level (N/N<sub>0</sub>), and the ratio of moment to shear force. There are different opinions about change of  $L_p$  when the height/length ratio ( $H_w/L_w$ ) ratio of the shear walls becomes greater than 2. However, there is no direct expression that takes into account the effect of the change of the  $H_w/L_w$  ratio on the plastic hinge length. For this reason, the  $H_w/L_w$  ratio was determined as a parameter in the study. Other parameters taken into account were axial load ratio (N/N<sub>o</sub>) and horizontal web reinforcement ratio ( $\rho_{sh}$ ). The codes provide limit values for these parameters, and their effects have been studied as they are crucial for determining the plastic hinge length in accordance with the actual behavior. In the study, nonlinear analyses were conducted on 72 different types of shear wall sections when the tested parameters were selected as  $L_{w}$ ,  $H_{w}$ ,  $N/N_{o}$ , and  $\rho_{sh}$ . Certainly, other factors may be effective in determining the behavior of shear walls. For example, wall thickness, slab type, slab-shear wall connection type are some of them. The plastic hinge height of shear walls was determined according to the heights of the deformations in the concrete and longitudinal steel reinforcement in the section when the shear walls lateral load decreased by 15%. The relationship between the findings of this study and empirical formulas in the literature was determined. Displacement ductility ( $\mu_{\delta}$ ) of shear walls were also determined with respect to selected parameters.

# 2. Description of plastic hinge

During an earthquake, reinforced concrete structures undergo non-linear deformations. It is assumed that nonlinear flexural deformations in buildings concentrate at the sections called plastic hinge (the assumption of lumped plastic damage), and the system behaves elastically in the remaining regions. This hypothesis is called the plastic hinge hypothesis (Kumbasaroğlu, 2010). The plastic hinge length of a shear wall modeled as a vertical cantilever as shown in Figure 1 can be calculated as the sum of the elastic displacement at yielding state at the top of the shear wall ( $\Delta_y$ ) and the plastic displacement arising from the rotation of the plastic hinge ( $\Delta_p$ ). The method of calculation of the rotation value is presented in Equation 1.

$$\Delta = \Delta_{y} + \Delta_{p} = \frac{\phi_{y} H_{w}^{2}}{3} + (\phi_{u} - \phi_{y}) L_{p} (H_{w} - 0.5L_{p})$$
(1)

In the above equation,  $Ø_y$  represents the yield curvature and  $Ø_u$  represents the final curvature, and the  $L_p$  component allows to determine the plastic hinge rotation angle. It is assumed that the plastic curvature is lumped in the middle of the  $L_p$ . For this reason, the total length was taken as ( $H_w$ -0.5 $L_p$ ) in the plastic displacement calculation.  $L_p$ , which is also defined as the observation length where sectional damages gather (where theoretical crush occurs in the concrete) after earthquakes, in fact does not exactly represent the point where plastification occurs. Within the section, the plastification starts from the point where the reinforcement yields. The height ( $L_{pz}$ ) of this area, where reinforcement begins to yield, can become higher than the length of the plastic hinge (Kazaz, 2013; Kazaz & Gülkan, 2012). However, it is impossible to observe this length from the outside. For this reason, strain gauges must be placed on the reinforcement. Priestley et al. (2007), Hoult et al. (2018) and Kazaz (2013) accepted the  $L_{pz}$  length as  $2L_p$  in their studies (Kazaz & Gülkan, 2012). Similarly, in this study,  $L_p$  was defined as the observed plastic hinge height and the  $L_{pz}$  was defined as the calculated (analytical) plastic hinge height. The main purpose of the study is to formulate the relationship between  $L_{pz}$  and  $L_p$  depending on changing shear wall parameters.



a)The Relationship of b) Shear Wall Section c) Curvature Diagram d) Idealized Curvature e) Load-Displacement Moment-Curvature Diagram Relationship

Figure 1. Plastic hinge method and definition of hinge length (authors).

Shear wall height is an important parameter in the plastification of shear walls. When the  $H_w/L_w$  ratio is greater than 2, bending behavior is generally observed for the shear wall. TBEC-2018 (2018) and other codes (ACI-318 (2019) ; Eurocode-8 (2004)) accepted the situation of ( $H_w/L_w$ ) ratio being equal to 2.0 as the limit state. In the literature there are different opinions about  $L_p$  when the  $H_w/L_w$  ratio of the shear walls becomes greater than 2. Kazaz & Gülkan (2012) developed Equation (2) to determine the plastic hinge length, taking into account other variables as well.

$$L_{p} = 0.27 L_{w} \left( 1 - \frac{N}{N_{0}} \right) \left( 1 - \frac{f_{y}}{f_{c}} \rho_{sh} \right) \left( \frac{M}{V} \right)^{0.45}$$
(2)

In Equation (2), N/N<sub>o</sub> is the axial load ratio at the base of shear wall,  $\rho_{sh}$  is horizontal web reinforcement ratio, M/V is moment to shear force ratio, L<sub>w</sub> is shear wall length, f<sub>c</sub> is concrete compressive strength, f<sub>y</sub> is reinforcement yield strength, and (M/V) /L<sub>w</sub> ratio takes into account shear wall's failure mode (bending, shearing, shearing / bending) and to some extent replaces the shearing stress. Biskinis & Fardis (2010) proposed Equation (3) for the members that have good seismic detailing.

$$L_{p} = 0.2L_{w} \left(1 + \frac{1}{3}\min\left(9, \frac{L_{s}}{L_{w}}\right)\right)$$
(3)

where, L<sub>s</sub>/L<sub>w</sub> ratio is the ratio of moment shearing force to shear wall width. Bohl and Adebar (2011) proposed Equation (4).

$$L_{p}=(0.2L_{w}+0.05L_{s})(1-1.5\frac{N}{A_{g}f_{c}}) \le 0.8L_{w}$$
(4)

where, N is axial load,  $A_g$  is shear wall area in earthquake direction. Eurocode8 (2004) proposes the plastic hinge length be determined by Equation (5).

$$L_{p} = \frac{L_{s}}{30} + 0.2L_{w} + 0.11 \frac{d_{bL}f_{y}(MPa)}{\sqrt{f_{c}(Mpa)}}$$
(5)

where,  $L_s$  is the shearing span (M/V),  $d_{bL}$  is average reinforcement diameter. Altheeb et al. (2015) used Equation (6) to determine the plastic hinge length. In the equation  $f_u$  is reinforcement ultimate strength and  $f'_c$  compressive strength of concrete.

$$L_{p} = \frac{(f_{u} - f_{y})d_{b1}^{2}}{4\sqrt{f_{c}^{2}}}$$
(6)

Aydın (2018) examined the plastic hinge lengths and displacement limits by considering the moment curvature relations of the shear walls. Zhi et al. (2019) examined behavior of reinforced concrete shear walls with continuous or lap-spliced bar connections in plastic hinge zones. Foroughi & Yüksel (2019) investigated the effects of different parameters on plastic hinge length and displacements through analytical models. Hashim et al. (2020) investigated the plastic hinge lengths of curtains by creating finite element models.

### 2.1. Relationship between critical shear wall height and plastic hinge length

If a reinforced concrete building contains shear walls, shear wall damage is primarily expected in an earthquake. Example shear walls that are damaged during earthquakes are shown in Figure 2. Figure 2b.(a) shows a shear wall damaged in 2011-Canterbury earthquake, Figure 2(b) shows a shear wall severely damaged in 2010-Maule earthquake and Figure 2(c) shows another shear wall severely damaged in 2010-Chile earthquake. Damages in Figure 2b.(b) and Figure 2b.(c) were caused by incorrect detailing of the shear walls (These shear walls have not been designed according to the relevant regulations). The aim of this study is to determine the  $L_p$  and  $L_{pz}$  lengths of the shear wall designed according to the codes. After the shear walls are damaged, the displacements will increase in the structures and frame elements starts to experience damage. If there is no strength to meet the displacement made by the shear wall at the column flange regions, there may be hinge development at column flanges and the situation may cause the structure to collapse. In order to prevent such a situation, the amount of bending displacements expected to occur in the plastic hinge zones, and the distribution of the damage must be taken into consideration during the design of ductile shear walls.



Figure 2a.Examples of reinforced concrete shear walls damaged after 2023 Kahramanmaraş Earthquake Doublet; (Oztürk et al. (2023).



Figure 2b. Examples of reinforced concrete shear walls damaged in earthquakes (Grossi et al., 2011); (Westenenk, B. et al., 2012).

In order to prevent the brittle collapse mechanism and limited ductility, the plastic hinge zones that may be formed should be properly detailed. In order for this detailing to be proper, the codes introduced some limits in the areas where they expect shear wall stresses to be maximum and defined the critical shear wall height. Table 1 shows the formulas for critical shear wall height in TBEC-2018 (2018) and ACI 31 (2019) and EC8 (2004) codes. The reinforcement distribution is denser along the critical height and it was required to create shear wall flange regions when the  $H_w / L_w$  ratio is greater than 2. In other words, if the ratio remains below 2, flexural hinging development is not expected in the shear wall.

ľa	<b>able 1.</b> Critical shear wall height limits determined by codes							
	References	Critical shear wall height (H <sub>cr</sub> ) limits						
	TBEC-2018	$2L_w \ge H_{cr} \ge max (l_w; H_w/6)$						
-	EC8-2005	$H_{cr} = max (L_w; Hw/6), 2L_w$						
		$H_{cr} \leq h_s  n \leq 6 \text{ stories}$						
		$2h_s$ n $\ge$ 7 stories						
	ACI- 318-2019	$H_{cr} = (L_w; M_u / 4V_u)$						

Table 1	Critical	shear	wall	height	limits	determine	d by	codes
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(Lw: Length of shear wall in the plan, Hw: Total shear wall height, hs: story height, n: number of stories, Mu: Moment value in shear wall section, Vu: Shearing force in shear wall section)

#### 2.2. Ductility and plastic hinge length

Ductility is the ability of a material, section, element, or a structural system to strain beyond the elastic limit, thus, to displace, without any significant change in stress, section force, or load. Plastic hinge length and, member and system ductility are closely associated with. The requirement of ductility is the formation of plasticization zones. Inel and Ozmen (2006) and, Arslan (2012) observed, in their studies, that the plastic hinge length affects the displacement capacity, consequently affectings the ductility. In Figure 3,  $F_u$  stands for the ultimate load,  $\delta_y$  for yield displacement where elastic behavior ends,  $\delta_u$  for ultimate displacement, and the numerical definition of ductility is expressed by Equation (7).

The accuracy of the models created for structures can be determined by load-displacement curves. Load displacement curves provide information about the behavior of structural elements. Figure 3 shows the information that can be determined with the help of the load-displacement curve along with ductility. The plastic hinge height of shear walls was determined according to the heights of the deformations in the concrete and longitudinal steel reinforcement in the section when the shear walls lateral load decreased by 15%. Displacement ductility ( $\mu_{\delta}$ ) of shear walls were also determined with respect to selected parameters.

For ductility comparison, the maximum displacements that the shear wall can achieve without any major loss in capacity are taken into account. Therefore, the ductility ratio is calculated as the ratio of the displacement value ( $\delta_u$ ) corresponding to 85% of the maximum load-carrying capacity attained by the beam to the displacement value at yielding ( $\delta_y$ ) for flexural RC elements. It is stated in the literature that the minimum value of this ratio for a RC member is around 4 ~ 5 (Ling et al. (2023)). Shear walls where shear behavior is effective on the other hand, ductility is quite limited since no ductile plateau will occur.



Figure 3. Energy dissipation capacity and load-displacement relationship.

# 3. Analytical study

In this present study, numerical analyses were performed using a finite element tool of ABAQUS to i) investigate the effects of the parameters on  $L_p$  and  $L_{pz}$  of ductile reinforced concrete shear walls, ii) determine the plastic hinge lengths of high-ductility shear walls, iii) evaluate the damages (crushing of concrete and yielding of steel) separately for concrete and reinforcement and to determine the relationship between  $L_p$  and  $L_{pz}$ , iv) determine displacement ductility of shear walls with respect to selected parameters. The parameters selected in the study to achieve these four objectives are explained below. The selected parameters are similar to the parameters studied in the literature. Slab thickness, concrete class, longitudinal reinforcement ratio, shear wall thickness, conditions in the connection area, etc. many parameters such as can also affect the results These parameters were kept constant due to the limits of the study.

In the experimental and analytical studies in the literature by Thomsen & Wallace (2004), Biskinis & Fardis (2010), Bohl & Adebar (2011), Kazaz & Gülkan (2012), the amount of the effect of these parameters was discussed and they proposed empirical formulas. The parameters included in the formulas are shown in Table 2. The parameters considered in this study and their ranges of variation are shown in Table 3. 72 shear wall models were examined in the current study.

Table 2. I arameters in formulas suggested in the interature (autions										
Litanatuma		Parameters								
Literature	$L_{w}$	$H_{\rm w}$	M/V	N/No	$oldsymbol{ ho}_{ m sh}$					
Thomsen an	nd Wallace (200	)4)	$\checkmark$							
Biskinis & I	Fardis (2010)		$\checkmark$		$\checkmark$					
Bohl ve Ade	ebar (2011)		$\checkmark$		$\checkmark$	$\checkmark$				
Kazaz & Gi	ilkan (2012)		$\checkmark$		$\checkmark$	$\checkmark$	$\checkmark$			
	Table 3. Sel	ected param	eters and the	ir ranges	s (authors	).				
-	Parameter	Min	Max	Step	of increas	e				
-	$H_w/L_w$	2	7		1					
	$oldsymbol{ ho}_{ m sh}$	0.0015	0.0035	C	0.0010					
_	N/N <sub>o</sub>	0.05	0.20		0.05					

Table 2. Parameters	in formulas	suggested in	the literature	(authors).
				(

#### 3.1. Design of the reinforced concrete shear walls

Calculations were made by taking the thickness of the shear walls ( $b_w$ ) as 0.25 m and the length of the shear walls in the plan ( $L_w$ ) as 1.75 m, by taking into consideration the cross-section limiting conditions given in TBEC-2018.

The shear wall models were created with the critical shear wall height ( $H_{cr}$ ) being 1.76 m for all shear walls whose  $H_w/L_w$  ratio is different from 2. In shear walls whose  $H_w/L_w$  ratio is greater than 2, flange regions were created. The length of the shear wall flanges was determined as 0.50 m along the critical shear wall height, and as 0.25 m above the critical shear wall height.

Steel reinforcement was determined using the minimum reinforcement ratios according to TBEC-2018. The design was made so that the longitudinal reinforcement is 16Ø10 in the shear walls with  $H_w/L_w=2$ . The reinforcement used in the shear walls whose  $H_w/L_w$  ratio is greater than 2 are given in Table 4. The details of a sample shear wall reinforcement whose  $H_w/L_w$  ratio is 4 is given in Figure 4.

Table 4.	Reinforcement used in shear walls whose $H_w / L_w$ ratio is greater than 2 (Aut						
	Location	$ ho_{ m lu}$	$ ho_{ m lw}$	$ ho_{ m sh}$			
	H <h<sub>cr</h<sub>	6Ø14	6Ø10	Ø10/42(0.0015) Ø10/25(0.0025)			
	H>H <sub>cr</sub>	4Ø14	10Ø10	Ø10/18(0.0035)			

**Table 4.** Reinforcement used in shear walls whose  $H_w / L_w$  ratio is greater than 2 (Authors).

 $(\rho_{lu}: flange longitudinal reinforcement at critical height, \rho_{lw}: flange reinforcement above critical height, \rho_{sh}: horizontal web reinforcement)$ 



Figure 4. Shear wall reinforcement detail (authors).

#### 3.2. Design of the reinforced concrete shear walls

Microscopic models are used to evaluate the behavior of the reinforced concrete shear walls. They take into account continuous mechanics and often include solutions with numerical processing procedures. Finite elements may be cited as examples for microscopic models (Marzok et al., 2020). Shear wall models were created within ABAQUS, which is commercial finite element software. The concrete part of the shear walls was modeled by using solid finite elements and their reinforcements were modeled with truss elements.

In the study, the concrete grade is chosen as C25 (compressive strength ( $f_{cd}$ ) is 25 MPa, and reinforcement type B420c (yield strength is 420 MPa). The formulas given in Dere (2017) were used for the compressive and tensile behavior of concrete. In Figures 5-6, uniaxial stress-strain curves are given for concrete and steel. The damage parameter referred to in CDPM material definition expresses the damage ratio, occurring in the element, with real numbers between 0-1. The relationship between the inelastic strain and the damage parameter of tensile and compressive behavior of concrete, were calculated based on the formulas given in Dere (2017). Figure 7 shows the damage parameter variation graph obtained for the concrete compression behavior. The TS500-2000 (2000) and ACI-318 (2019) codes accept the strain corresponding to the uniaxial compressive strength of the concrete as 0.003 for all concrete grades. A confined concrete model has not been created since the lateral web reinforcements inside the shear wall and stirrups at the wall flange regions are modeled in ABAQUS. Therefore, the web concrete was modeled as unconfined. In other words, the reinforcement is already defined in the model, the behavior of confined and unconfined concrete emerges in the ABAQUS model.



Figure 5. Uniaxialstress-strain relationship of concrete ; (a) for compression, (b) for tension (authors).



Load definitions were made so that  $N/N_0$  become 0.05, 0.1, 0.15, and 0.2. The supports were arranged as fixed supports. Top horizontal displacements of the shear walls considered in plastic hinge length calculation were determined according to the displacement corresponding to the collapse of the shear wall.

Damage modes of shear walls can be divided into two types: in-plane and out-of-plane damage. Due to the earthquake effect, most of the shear walls exhibited in-plane damage. However, there are shear walls that are damaged out of plane under certain earthquakes. For shear walls with small thicknesses, out-of-plane damage may occur even when the inter-story deformation in the out-of-plane direction is small (Cheng et al. (2023)). Robazza et al. (2018), El-Hashimy et al. (2020) and Wang et al. (2021), examined the out-of-plane behavior of shear walls. However, existing studies and finite element analyzes less consider the contribution of the out-of-plane stiffness of shear walls (Wei et al. (2017)). In this study, out-of-plane behavior is neglected.

A mesh sensitivity analysis was carried out in order to optimize maximum solid finite element size. The finite element mesh size was changed from 30 mm to 80 mm as presented in the table. In the example analysis, the top surface of the shear wall was subjected to a 20 mm lateral displacement, and a nonlinear pushover analysis was carried out. The results for all mesh configurations were presented in the Table 5. As it is seen, the base shear obtained from config #1 and config #3 are quite close. The concrete material used in the analyses is nonlinear and therefore the variation of the base shear is not as expected to be (as the number of nodes increases). The analysis of config #1 took around 11 hours whereas the analysis of config #3 took around 2 hours and 40 minutes. Therefore config #3 was found to be accurate enough and convenient in terms of computation time. Truss reinforcement elements were divided into 0.05 m wide finite elements (Figure 8).

Mesh	Maximum	Number	Number of	Top edge	Base shear
configuration	element	of	elements	displacement	(kN)
No.	size (mm)	nodes		(mm)	. ,
1	30	221021	195952	19.5362	157.967
2	40	102941	88620	19.5347	159.610
3	50	59848	50641	19.5366	157.656
4	60	38376	32010	19.5349	159.796
5	70	30796	25919	19.5356	159.758
6	80	22723	19022	19.5349	160.310

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In order to be able to perform the displacement-controlled analysis of the modeled shear walls the displacement loading was applied monotonically. The assumption of complete bond between concrete and reinforcement has been made. The displacement contour was used to determine the value of concrete damage occurring in the pressure zone. Coloring in the output was examined for damage parameters corresponding to inelastic strain of 0.003 and larger.



Figure 8. Dividing the shear wall model into finite elements (authors).

The accuracy of the used software and the created models were checked against the experimental results of the RW2 shear wall test with an  $H_w/L_w$  ratio of 3 conducted by Thomsen and Wallace (2004) (Figure 9 and Figure 10). An axial load of  $0.07A_gf_c$  was applied at the top of the RW2 shear wall. In additon lateral displacements was applied to the top of the shear wall. As a result of the experiment, the damage situation occurred when the RW2 shear wall makes 2.5% drift is shown in Figure 10 (Thomsen & Wallace, 2004). As can be seen in the ABAQUS model, 15% strength loss after maximum lateral load corresponds to 2-2.5% lateral displacement ratio.



Figure 9. RW2 shear wall cross-sectional view (Thomsen & Wallace, 2004).



Figure 10. Comparison of load displacement curves-RW2 and RW-2 damage-2.5% drift. (Thomsen & Wallace, 2004).

Load-displacement curves of the modeled shear walls were obtained. In determining the plastic hinge lengths the horizontal displacement level at the moment when the maximum load decreases by 15% which is assumed to correspond to the collapse of the shear wall was used.

Considering the damages occurred in the reinforcement and concrete at the determined displacement values, the plastic hinge lengths for the shear walls were determined as two different height values,  $L_p$  and  $L_{pz}$  (Figure 11 and Figure 12).



Figure 11. L<sub>pz</sub> and L<sub>p</sub>'s theoretical illustration on the shear wall (authors).



Figure 12. Illustration of the plastic hinge lengths on the shear wall model; (a)L<sub>p</sub>, (b)L<sub>pz</sub> (H<sub>w</sub>/L<sub>w</sub> 7-p<sub>sh</sub> 0.0035-N/N<sub>o</sub> 0.15) (authors).

# 4. Research results

The plastic hinge lengths, evaluated for each shear wall at the determined displacement values, were calculated as  $L_p$  and  $L_{pz}$ . Examples of damage situations taken into account when determining  $L_p$  values are shown in Table 6 and Table 7. In the tables arranged according to the N/N<sub>0</sub> ratio, it is seen that the concrete damages are concentrated in the pressure zone of the shear walls. However, at low load level (N/N<sub>0</sub>=0.05), deformation also occurred in the concrete in the tension zone. Load level change causes changes in damage distribution. It is seen that as the N/N<sub>0</sub> ratio increases, the damage occurs in a narrower area.  $L_p$  lengths were determined according to the damage status of the outermost fiber in the concrete. The effect of horizontal web reinforcement ratio could not be observed in the damage patterns, since the behavior of unconfinement concrete was observed in the outermost fiber of the concrete.



**Table 7.** Examples of damage cases when  $\rho$ sh value is 0.0035 for  $L_p$  (Authors)



Hw/Lw=2

-Hw/Lw=3

Hw/Lw=4 Hw/Lw=5

-Hw/Lw=6

-Hw/Lw=

1800 2000

1600

The load-displacement curves obtained as a result of the analyzes were grouped according to  $N/N_o$  ratio. It has been observed that as the  $N/N_o$  ratio increases, the values in shear wall capacity increase. The curves include all  $H_w/L_w$  ratios considered. As the  $H_w/L_w$  ratio increased, shear wall capacities decreased. The load-displacement curves of walls with  $N/N_o$  ratio of 0.05 are shown in Figure 13-15.



Figure 13.  $\rho_{sh} = 0.0015$ , N/N<sub>o</sub>=0.05 load-displacement curves.

Figure 14.  $\rho_{sh} = 0.0025$ , N/N<sub>o</sub>=0.05 load-displacement curves.



Figure 15.  $\rho_{sh} = 0.0035$ , N/N<sub>o</sub>=0.05 load-displacement curves.

The load-displacement curves of walls with N/No ratio of 0.1 are shown in Figure 16-18.



Figure 16.  $\rho_{\rm sh} = 0.0015$ , N/N<sub>o</sub>=0.10 load-displacement curves.



Figure 17.  $\rho_{sh} = 0.0025$ , N/N<sub>o</sub>=0.10 load-displacement curves.



The load-displacement curves of walls with N/No ratio of 0.15 are shown in Figure 19-21.



Figure 19.  $\rho_{\rm sh} = 0.0015$ , N/N<sub>o</sub>=0.15 load-displacement curves.

Figure 20.  $\rho_{sh} = 0.0025$ , N/N<sub>o</sub>=0.15 load-displacement curves.



**Figure 21.**  $\rho_{sh} = 0.0035$ , N/N<sub>o</sub>=0.15 load-displacement curves.

The load-displacement curves of walls with N/No ratio of 0.2 are shown in Figure 22-24.



Figure 22.  $\rho_{sh} = 0.0015$ , N/N<sub>0</sub>=0.20 load-displacement curves. Figure 23.  $\rho_{sh} = 0.0025$ , N/N<sub>0</sub>=0.20 load-displacement curves.



Figure 24.  $\rho_{\rm sh} = 0.0035$ , N/N<sub>o</sub>=0.20 load-displacement curves.

The  $L_p$  values, obtained when the maximum load decreased by 15% (0.85Fmax), were taken into account and the graphs were drawn up so that the vertical axis is  $L_p/L_w$  and the horizontal axis is  $H_w/L_w$ . The graphs grouped according to  $\rho_{sh}$  are shown in Figure 25-27. In each graph, the changes in the relations can be observed depending on N/N<sub>o</sub> ratios. The 0.5L<sub>w</sub> limiting value stated in TBEC-2018 for plastic hinge length is shown in the graphs.

The change of  $L_p$  depending on  $\rho_{sh}$  is shown in Table 8. It is seen that the horizontal web reinforcement is not a very effective parameter in the plastic hinge length. In Table 9,  $(L_p/L_w)_{avg}$  values are given according to shear spans.



**Figure 25.**  $H_w/L_w$  -  $L_p/L_w$  graph for  $\rho_{sh} = 0.0015$  (authors).



**Figure 26.**  $H_w/L_w - L_p/L_w$  graph for  $\rho_{sh} = 0.0025$  (authors).



**Figure 27.**  $H_w/L_w - L_p/L_w$  graph for  $\rho_{sh} = 0.0035$  (authors).

Parameters		Horizon $(\rho_{\rm sh})$	ntal We	o Reinf	orcement	Ratio
		0.0015	0.0	025	0.0035	
$\left(\frac{Lp}{Lm}\right)_{avg}$		0.258 0.27		78	0.249	
LW <sup>2</sup>						
Table 9. ( Parameter	L <sub>p</sub> /L <sub>w</sub> ) <sub>ort</sub> v	values acc S	cording t shear Spa	o shear s n (H <sub>w</sub> /L	pan (auth w)	ors).
Table 9. ( Parameter	$\frac{L_p/L_w)_{ort}}{2}$	values acc S	cording t Shear Spa 4	o shear s n (H <sub>w</sub> /L 5	pan (auth w) 6	ors). 7

Table 8. (L<sub>p</sub>/L<sub>w</sub>)<sub>avg</sub> values according to horizontal web reinforcement ratios (authors).

When the graphs drawn up by considering the limit state are examined, it is observed that  $L_p$  values generally increase as N/N<sub>o</sub> ratio decreases and as  $H_w/L_w$  ratio increases. It is seen that the  $\rho_{sh}$  change causes small differences and is not a very effective parameter. The value given for the plastic hinge length in TBEC-2018 is 0.5L<sub>w</sub>, and in the study, it was seen that plasticization occurred around 0.25-0.29L<sub>w</sub>. It is seen that the  $L_p$  length of the 72 shear walls analyzed within the limits in this study does not exceed the regulation limits. This shows that the code is based on a higher plastic length than the observed plasticization. On the other hand, a comparison was made according to  $L_{pz}$  values in Fig. 16-Fig-18. For each scenario taken as basis, a value greater than the plastic hinge length accepted by the code was found. For this reason, it is seen that TBEC-2018 actually defines the length of plastic hinge at a level between  $L_p$  and  $L_{pz}$ . According to the values given in Table 8 and Table 10, it is observed that  $L_p$  and  $L_{pz}$  vary in the 0.224~1.08 band.

 $L_{pz}$  obtained when the maximum load decreases by 15% were taken into consideration and the  $H_w/L_w$  vs.  $L_{pz}/L_w$  graphs were drawn up (Figures 28-30).



**Figure 28.**  $H_w/L_w$  -  $L_{pz}/L_w$  graph for  $\rho_{sh} = 0.0015$  (authors).



**Figure 29.**  $H_w/L_w - L_{pz}/L_w$  graph for  $\rho_{sh} = 0.0025$  (authors).



**Figure 30.**  $H_w/L_w L_{pz}/L_w$  graph for  $\rho_{sh} = 0.0035$ (authors).

The effect of the ratio of N/N<sub>o</sub> on the ratio of  $L_{pz}/L_w$  is much higher especially for the shear walls with high web reinforcement ratio ( $\rho_{sh}$ =0.0035). The decrease in the ratio of N/N<sub>o</sub> ratio increases  $L_{pz}$  value dramatically for high H<sub>w</sub>/L<sub>w</sub> ratios. The change in  $L_{pz}$  with respect to  $\rho_{sh}$  is given in Table 10. Depending on the change of H<sub>w</sub>/L<sub>w</sub> ratio, ( $L_{pz}/L_w$ )<sub>avg</sub> values are shown in Table 11.

Table 10. (L <sub>pz</sub> /L <sub>w</sub> ) <sub>avg</sub> values according to horizontal web reinforcement ratios (authors).								
	Horizontal Web Reinforcement Ratio							
Paramete	er		$( ho_{ m sl})$	n)		_		
	0.0015 0.0025 0.0035							
$\left(\frac{Lpz}{Lw}\right)_{avg}$		0.938	0.937	1	0.954	_		
Table 11. (L <sub>pz</sub> /I	<b>Table 11.</b> $(L_{pz}/L_w)_{avg}$ values according to shearing opening (auth							
Parameter	Shear span (H <sub>w</sub> /L <sub>w</sub> )							
	2	3	4	5	6	7		
$\left(\frac{\text{Lpz}}{\text{Lw}}\right)_{\text{avg}}$ (	).754	0.856	0.959	1.006	1.004	1.08		

 $L_{pz}$  values decrease as N/N<sub>o</sub> ratio increases. However,  $L_{pz}$  values increase as  $H_w/L_w$  ratio increases. The change in  $\rho_{sh}$  causes only small differences when the maximum load decreases by 15% and is not a very effective parameter. The  $L_p/L_{pz}$  and  $H_w/L_w$  ratios were determined by considering the plastic hinge lengths obtained depending on the  $\rho_{sh}$  ratio (Figure 31-33).



**Figure 31.**  $H_w/L_w - L_p/L_{pz}$  graph for  $\rho_{sh} = 0.0015$  (authors).



**Figure 32.**  $H_w/L_w$  -  $L_p/L_{pz}$  graph for  $\rho_{sh} = 0.0025$ (authors).



**Figure 33.**  $H_w/L_w - L_p/L_{pz}$  graph for  $\rho_{sh} = 0.0035$  (authors).

It is seen that  $L_p$  and  $L_{pz}$  is related with a ratio between 0.25 and 0.4. This ratio is considered as 0.5 in the literature.

#### 4.1. Ductility

The ductility ( $\mu$ ) values were determined and the H<sub>w</sub>/L<sub>w</sub> vs.  $\mu$  graphs were created by using the displacements determined according to both the crushing occurred in the shear wall concrete and the yield observed in the steel reinforcement (Figure 34-36). Displacement ductility was determined according to the load-displacement graphs obtained for 72 walls (given in groups above, Fig 13-23). When the changes in the obtained ductility are examined, displacement ductilities ranging from 5.77 to 8.78 are observed. Of course, factors such as keeping the normal force quite limited in the study and neglecting the out-of-plane behavior of the walls caused a relative increase in ductility.



**Figure 34.** H<sub>w</sub>/L<sub>w</sub> -  $\mu$  graph for  $\rho_{sh} = 0.0015$  (authors). **Figure 35.** H<sub>w</sub>/L<sub>w</sub> -  $\mu$  graph for  $\rho_{sh} = 0.0025$  (authors).



**Figure 36.**  $H_w/L_w$  -  $\mu$  graph for  $\rho_{sh} = 0.0035$  (authors).

The change in  $\mu$  with respect to  $\rho_{sh}$  is given in Table 12. Depending on the change of  $H_w/L_w$  ratio,  $(\mu)_{avg}$  values are shown in Table 13.

	Parameter	HOLIZOIII	a web Kelli	lorceme	ni Katio		
	1 aranıc						
			0.0015	0.0025		0.0035	
	(μ) <sub>av</sub>	g	6.72	6.77		7.52	_
Table 13	. (μ) <sub>avg</sub> valu	es acco	rding to hori	zontal web 1	reinforce	ment ratio	os (authors).
Par	rameter		2	Shear span (	H <sub>w</sub> /L <sub>w</sub> )		
_		2	3	4	5	6	7
(	μ) <sub>avg</sub>	6.2	8.78	7.5	7.3	6.5	5.77

**Table 12.**  $(\mu)_{avg}$  values according to horizontal web reinforcement ratios (authors).

In order for the structure to exhibit ductile behavior, it must undergo plastic deformation. Since plastic hinge length and ductility are closely related, the effects of the parameters whose effects on plastic joint length were examined on ductility were also examined. It was observed that the ductility value increased as the horizontal confinement reinforcement increased. The confinement effect had a positive impact on ductility. The increase in the  $H_w/L_w$  ratio generally caused an increase in  $L_p$  and  $L_{pz}$  values. It can be said that as the  $H_w/l_w$  ratio increases, the deformations increase in the concrete and reinforcement. However, it has been observed that the ductility ratio decreases as the  $H_w/L_w$  ratio increases (except  $H_w/L_w=3$ ). As the  $N/N_o$  ratio decreases, the ductility value ( $\mu$ ) becomes more dependent on the  $H_w/L_w$  ratio. This is more apparent especially in the shear walls having very low normal force ( $N/N_o = 0.05$ ) and partially for ( $N/N_o = 0.1$ ). It is also seen from the graphs that the ductility is inversely related with  $H_w/L_w$  ratio when  $N/N_o$  is less than 0.1.

# 4.2. Comparison of the plastic hinge lengths

The literature contains various empirical formulas for determining shear wall plastic hinge lengths and the values obtained from these equations having high number of parameters were compared with the values obtained from the finite element analyses. The comparisons were carried out the formulas proposed by EC8-2004, Biskinis and Fardis (2010) Bohl and Adebar (2011) and, Kazaz and Gülkan (2012). Both the observed plastic hinge lengths ( $L_p$ ) and the analytical plastic hinge lengths ( $L_{pz}$ ) were included in these comparisons. Linear curve fitting is performed and the results are shown in Figures 37-40.

The comparisons given between Figure 25 and Figure 28 were made with the results obtained from  $L_p$  formulations in the literature. The results obtained from the ABAQUS model were compared with the  $L_p$  values in the literature, within accepted limits. The point that should be noted here is that plastic hinge is stated as  $l_p$  in the literature. However, in this study, two different plastic hinge lengths were determined. For this reason, both hinge lengths obtained from this study were compared with each approach.

First of all, for each approach, it is seen that  $L_p$  matches better with the approaches in the literature compared to  $L_{pz}$ . When the  $R^2$  values obtained from the linear regression are examined, it is seen that the best fit for the plastic hinge lengths is achieved with the study of Kazaz (2013). As shown in Figure 28, there is 78% good-fit between the values of Kazaz & Gülkan (2012) and the observed plastic hinge length values.











Figure 39. Comparison of Bohl & Adebar (2011); (a) with L<sub>p</sub>, (b) with L<sub>pz</sub> (authors).





#### 5. Conclusions and comments

Past earthquakes have shown that the inelastic energy-consuming capacity of a shear wall is very high. For this reason, shear walls are very effective in the performance shown by the shear walled structures during an earthquake. The length of the plastic hinge that develops in the region where shear wall meet foundation depend on the dimensions and details of the shear wall. The earthquake codes make a rather simplified assumption for the length of the plastic hinge that it would depend only on the length of the shear wall in the plan and be equal to  $0.5L_w$ . However, in the literature, there are many empirical formulas whereby the plastic hinge length of a shear wall can be calculated. In order for the plastic hinge to emerge, the reinforcement must begin yielding.

The mechanism is realized as a result of the concrete being crushed by making excessive deformations. Therefore, regarding the plastic hinge length, there are different heights definitions: the height at which the concrete is crushed ( $L_p$ ) and the hight at which the reinforcement starts yielding ( $L_{pz}$ ). While  $L_p$ , which represents the region where concrete crushed, can be observed from the outside,  $L_{pz}$  cannot clearly be observed most of the time. In this study, a series of analytical studies were carried out in order to determine the relationship between  $L_p$  and  $L_{pz}$ , to identify the parameters affecting the plastic hinge length, and to compare them with the empirical approaches available in the literature. The following results were obtained from the analyses;

- 1) In the analyses conducted; it is seen that L<sub>p</sub> and L<sub>pz</sub> lengths increase as H<sub>w</sub>/L<sub>w</sub> ratio increases, and that ρ<sub>sh</sub> change causes small differences in the case the maximum load decreasing by 15% and therefore, it is not a very effective parameter. It can be concluded that as the H<sub>w</sub>/L<sub>w</sub> ratio increases, the plastic deformations occurring in concrete and reinforcement increase. L<sub>p</sub> were determined based on the height of observed the crush as of the foundation top level in the concrete shear wall model. It can be stated that ρ<sub>sh</sub> change is not an effective parameter for L<sub>p</sub>, because there is no confinement effect on the observed concrete damage. For L<sub>pz</sub>, this situation can be explained by the fact that there are wall flange zones along the critical wall height and the reinforcement damage remains in this region. The axial force level has different effects: L<sub>p</sub> values increase as N/N<sub>o</sub> ratio decreases and as H<sub>w</sub>/L<sub>w</sub> ratio increases. It is seen that L<sub>pz</sub> values decrease as N/N<sub>o</sub> ratio increases. As the N/N<sub>o</sub> ratio decreased, the deformation ability of concrete and reinforcement increased. When the damages occurring in concrete is examined, as N/N<sub>o</sub> increases, the damage occurs in a narrower area. This situation can be interpreted as a decrease in ductility.
- 2) The value given for the plastic hinge length in TBEC-2018 is 0.5L<sub>w</sub>, and in the study, it was seen that plasticization occurred around 0.25-0.29L<sub>w</sub>. There are many different parameters that affect the height of the plastic hinge. However, considering the effects of the parameters examined, it was seen that the code remained on the safe side.
- 3) It is seen that  $L_p$  and  $L_{pz}$  are related with a ratio of 0.25-0.4 for the displacement limit. The literature states this ratio as 0.5. The plastic hinge length values remained between the critical shear wall heights determined by the codes. This situation can be interpreted as preventing limited ductility. The fact that the  $L_{pz}$  length is greater than the  $L_p$  length indicates that the damage occurred in the reinforcement, which is more ductile than the concrete.
- 4) As the N/N<sub>o</sub> ratio decreases, the ductility value ( $\mu$ ) becomes more dependent on the H<sub>w</sub>/L<sub>w</sub> ratio. This is considerably felt especially in the shear walls having very low normal force (N/N<sub>o</sub> = 0.05 and partially N/N<sub>o</sub> = 0.1). It is also seen from the graphs that the ductility is inversely related to H<sub>w</sub>/L<sub>w</sub> ratio when N/N<sub>o</sub> is less than 0.1. Examining the analysis results of the modeled shear walls, it is observed that the displacement ductility values decrease as the normal force value increases. The average ductility values of the shear walls, whose H<sub>w</sub>/L<sub>w</sub> (shear span) ratio is 2, are lower than the average ductility values of other modeled shear walls. It was observed that the ductility value was greater if the p<sub>sh</sub> value was 0.0035. This may be associated with the confinement effect.
- 5) In the literature, there are empirical formulas to determine plastic hinge lengths, and values obtained from equations with a high number of parameters have been compared with values obtained from analyses. When the  $R^2$  values obtained from the linear regression are examined, it is seen that the best fit for the plastic hinge lengths is achieved with the study of Kazaz (2013). The accuracy of the Kazaz approach in predicting  $L_p$  and  $L_{pz}$  values obtained by this study is 78% and 69%, respectively. It was observed that there is better agreement between the plastic hinge values obtained from the studies and the observed plastic hinge length values compared to the agreement between the plastic hinge values obtained from the studies and the analytical plastic hinge values. This finding also shows that the empirical formulas in the literature might be obtained considering the crushing of concrete.
- 6) Although the horizontal web reinforcement ratio does not have an effect on the plastic hinge formation and height, it is recommended by the building and seismic codes that it should be kept at a lower limit of 0.0025 to ensure that no shear damage occurs before the bending damage in the web. Similarly, since the axial force is an important factor in

the plastic hinge formation and the ductility capacity, the  $N/N_0$  ratio is limited to the upper limit of 0.35 in the codes. There is no upper limit except for the lower limit for the  $H_w/L_w$  ratio being greater than 2.0.

The results of the 72 shear walls modeled in the study can be further expanded in future studies according to the selected parameters. In this study, an evaluation was made on the parameters  $H_w/L_w$ ,  $N/N_o$ , and  $\rho_{sh}$ , which are effective in shear wall behavior. Certainly, other factors may be effective in determining the behavior of shear walls. For example, wall thickness, slab type, slab-shear wall connection type are some of them. In addition, there are other which would affect the shear wall behavior such as bond-slip of the reinforcement Kazaz (2012), cyclic loading (Pokhrel & Bandelt, 2019) and the presence of slabs between the stories (He et al., 2020; Surumi et al., 2015). In future studies, machine learning-based soft computing applications can also be made using shear wall models obtained with wide range parameters. Using different machine learning methods with planned studies, predict the length of the plastic hinge will be suggested. In future studies, deriving a new analytical formula and comparing it with existing ones, in which the effects of all parameters are evaluated, could be a worth-while way.

In reinforced concrete structures, shear walls are connected with slabs at story levels. In the studies to be developed, the behavior can be determined by adding slabs that will limit the horizontal displacement to the shear walls during the modeling phase. In the study, shear wall models were modeled as cantilever. In future studies, coupled wall models can be created and the differences between their behaviors can be examined.

The results obtained in this study were compared with the traditional results used in the literature. Ultimately, each plastic hinge model in the literature is an approach. However, in this study conducted on 72 walls, the  $L_p$  and  $L_{pz}$  lengths obtained may be more descriptive than the theoretical relations in the literature, since the section where the concrete is crushed and the reinforcement yielded can be determined from advanced non-linear FEM analyses. But the distribution of the parameters selected in this study, the range of changes, the limits in the analysis, etc. of course, this also limits their accuracy. Therefore, in future studies, comparisons can be made more sensitive with more shear wall parameters and different analysis options. The most important reason for the destruction caused by the earthquakes that occurred in Turkey on February 6, 2023, more than 50,000 people died and causing economic losses of nearly ten billion dollars, is the absence of well-designed (the seismic code design criteria proper) shear walls in reinforced concrete buildings. Therefore, studies conducted in the coming years regarding reinforced concrete shear walls will provide valuable insights for reinforced concrete buildings with better earthquake behavior.

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